

ECE 580 Optimization Methods for Systems and Control

Tentative Syllabus

The chapter and section titles, along with the chapter, section, and page numbers, refer to the text by Chong and Zak.

Part 1: Mathematical Review, Chapters 1, 2, 3, and 5, cover undergraduate mathematics. Students should carefully review these chapters to make sure that they are able to understand and use this material. Students are welcome to ask questions of the instructor regarding this material by email or by appointment. Chapter 4 will be covered in this course, as needed.

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